

Directions: Write the equation of variation for each situation, use k as the constant of variation.

1) F is inversely proportional to x

$$F = \frac{k}{x}$$

2) R is jointly proportional to S and T .

$$R = kST$$

3) R varies directly as m and inversely as the square of d .

$$R = \frac{km}{d^2}$$

4) Kinetic energy, E , is directly proportional to the square of the velocity, v and the mass m .

$$E = kv^2m$$

Directions: Write the equation of variation for each situation and solve.

5) U varies directly as the square root of v . (if $u=3$ when $v=4$)
find u when $v=10$.

$$\begin{aligned} \textcircled{1} \quad u_1 &= k\sqrt{v_1} \\ 3 &= k\sqrt{4} \\ 3 &= k(2) \\ \frac{3}{2} &= k \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad u_2 &= k\sqrt{v_2} \\ u_2 &= \frac{3}{2}\sqrt{10} \end{aligned}$$

6) Y varies directly as the cube of x . (if $y=48$ when $x=4$, find y when $x=8$.)

$$\begin{aligned} y_1 &= kx_1^3 \\ 48 &= k(4)^3 \\ 48 &= k(64) \\ \frac{48}{64} &= k \\ \frac{3}{4} &= k \end{aligned}$$

$$\begin{aligned} y_2 &= kx_2^3 \\ y_2 &= \frac{3}{4}(8)^3 \\ y_2 &= \frac{3}{4}(512) \\ y_2 &= 3 \cdot 128 \\ y_2 &= 384 \end{aligned}$$

7) Q varies jointly as m and the square of n , and inversely as P .
(if $Q=2$ when $m=3$, $n=6$, and $P=12$), find Q when $m=4$, $n=18$, and $P=2$.

$$\begin{aligned} Q_1 &= \frac{km_1n_1^2}{P_1} \\ 2 &= \frac{k(3)(6)^2}{12} \\ 2 &= \frac{k \cdot 3 \cdot 36}{12} \\ 2 &= 9k \\ \frac{2}{9} &= k \end{aligned}$$

$$\begin{aligned} Q_2 &= \frac{km_2n_2^2}{P_2} \\ Q_2 &= \frac{\frac{2}{9}(4)(18)^2}{2} \\ Q_2 &= \frac{8(324)}{2} \\ Q_2 &= \frac{8 \cdot 36}{2} \\ Q_2 &= 8 \cdot 18 \\ Q_2 &= 144 \end{aligned}$$

8) W varies jointly as x , y and z . If $w=36$ when $x=2$, $y=8$, and $z=12$, find w when $x=1$, $y=2$, and $z=4$.

$$\begin{aligned} W_1 &= kx_1y_1z_1 \\ 36 &= k(2)(8)(12) \\ 36 &= 192k \\ \frac{36}{192} &= k \\ \frac{3}{16} &= k \end{aligned}$$

$$\begin{aligned} W_2 &= kx_2y_2z_2 \\ W_2 &= \left(\frac{3}{16}\right)(1)(2)(4) \\ W_2 &= \frac{3}{2} \end{aligned}$$

Directions: Translate each statement into an equation using k as the constant of variation.

9) The length of time, t , that it takes fruit to ripen is inversely proportional to the sum, T , of the average daily temperatures during the growing season.

$$t = \frac{k}{T}$$

10) The maximum safe load, L , for a horizontal beam varies jointly as its width, w , and the square of its height, h , and inversely as its length, x .

$$L = \frac{Kwh^2}{x}$$

11) The number, N , of long-distance phone calls between two cities varies jointly as the populations P_1 and P_2 of the two cities, and inversely as the distance, d , between the two cities.

$$N = \frac{K P_1 P_2}{d}$$

12) The erosive force, P , of a swiftly flowing stream is directly proportional to the sixth power of the velocity, v , of the water.

$$P = K v^6$$

Directions: Write the equation of variation for each situation and solve.

13) The weight, w , of an object on or above the surface of the Earth varies inversely as the distance, d , between the object and the center of the Earth. If a girl weighs 100 pounds on the surface of the Earth, how much would she weigh 400 miles above Earth's surface? Assume the radius of the Earth is 4,000 miles, d_1

$$w_1 = \frac{K}{d_1}$$

$$100 = \frac{K}{4000}$$

$$400,000 = K$$

$$w_2 = \frac{K}{d_2}$$

$$w_2 = \frac{400,000}{4400}$$

$$w_2 = 90.9 \text{ lbs}$$

14) Ohm's Law states that the current, I , in a wire varies directly as the electromotive forces, E , and inversely as the resistance, R . If $I = 22$ amperes when $E = 110$ volts and $R = 5$ ohms, find I if $E = 220$ volts and $R = 11$ ohms.

$$I_1 = \frac{K E_1}{R_1}$$

$$22 = \frac{K(110)}{5}$$

$$22 = K(22)$$

$$1 = K$$

$$I_2 = \frac{K E_2}{R_2}$$

$$I_2 = \frac{220}{11}$$

$$I_2 = 20 \text{ amp}$$

15) If the amount of time, t , it takes Sully to complete one unit of Pre-Calc varies jointly as the number of sections, s and the number of mastery checks per section, m , and inversely as the square root of the number of problems per section, p and $t = 12$ when $s = 3$, $m = 2$, and $p = 64$, find t when $s = 5$, $m = 2$, and $p = 25$.

$$t_1 = \frac{K s_1 m_1}{\sqrt{p_1}}$$

$$12 = \frac{K(3)(2)}{\sqrt{64}}$$

$$12 = \frac{K(6)}{8}$$

$$96 = 6K$$

$$16 = K$$

$$t_2 = \frac{K s_2 m_2}{\sqrt{p_2}}$$

$$t_2 = \frac{16(5)(2)}{\sqrt{25}}$$

$$t_2 = \frac{16(5)(2)}{5}$$

$$t_2 = 32 \text{ hours}$$

16) The electrical resistance, R of a wire varies directly as its length and inversely as the square of its diameter. A wire with a length of 200 inches and a diameter of one-quarter of an inch has a resistance of 20 ohms. Find the electrical resistance in a 500 inch wire with the same diameter.

$$R_1 = \frac{K l_1}{d_1^2}$$

$$20 = \frac{K(200)}{(\frac{1}{4})^2}$$

$$20 = \frac{K(200)}{\frac{1}{16}}$$

$$20 = 3200K$$

$$\frac{20}{3200} = K$$

$$\frac{1}{160} = K$$

$$R_2 = \frac{K l_2}{d_2^2}$$

$$R_2 = \frac{160(500)}{(\frac{1}{4})^2}$$

$$R_2 = \frac{50}{\frac{1}{16}}$$

$$R_2 = 50 \text{ ohms}$$