

# Graphs & Inverses of Trig Functions

## 6 - Graphing Secant & Cosecant

### Periodic Function

A function in which for some real number  $\alpha$ ,  $f(x + \alpha) = f(x)$  for each  $x$  in the domain of  $f$ .

$$y = A \sec [K(\theta - PS)] + VD$$

$$y = A \csc [K(\theta - PS)] + VD$$

### A

$A$  = the coefficient of the trig function. This determines the vertical stretching and shrinking of a graph. It also determines if the graph is reflected over the midline.

### Amplitude

Amplitude of Sine and Cosine =  $|A|$  = half the distance between the minimum and maximum values of the range of a periodic function with a bounded range.

### Vertical Displacement

$VD$  = the vertical translation

### Midline

The horizontal axis used as the reference line about which the graph of a periodic function oscillates.

### Period

$P$  = the horizontal length of the unique part of the graph.

### Phase Shift

$PS$  = the horizontal translation.

### Domain for trig functions

all the angles that can be put into the function (all the numbers included from left to right).

### Range for trig functions

all the values that come out of the function (all the numbers included from bottom to top).

How to determine all the important things...

$$y = A \sec [K(\theta - PS)] + VD$$

A:  $A$

~~Amplitude:~~

Reflected over midline?

Vertical Displacement:  $\circ$

Midline:  $y = 0$

Phase Shift:  $PS$

Period:  $\frac{360^\circ}{K}$

$$y = A \csc [K(\theta - PS)] + VD$$

A:  $A$

~~Amplitude:~~

Reflected over midline?

Vertical Displacement:  $\circ$

Midline:  $y = 0$

Phase Shift:  $PS$

Period:  $\frac{2\pi}{K}$

## Graphs &amp; Inverses of Trig Functions

## 6 - Graphing Secant &amp; Cosecant

State the essentials for each function.

#1)  $y = 10 \sec\left(\frac{1}{2}\theta - 45^\circ\right) + 3$

$$y = 10 \sec\left[\frac{1}{2}(\theta - 90^\circ)\right] + 3$$

A: 10

~~Amplitude:~~

Reflected over midline? No

Vertical Displacement: 3

Midline:  $y = 3$

Phase Shift:  $90^\circ$

Period:  $\frac{360^\circ}{\frac{1}{2}} = 720^\circ$

$$y = -243 \csc\left[\frac{1}{3}\left(\theta + \frac{3\pi}{4}\right)\right] - 2$$

#2)  $y = -243 \csc\left(\frac{1}{3}\theta + \frac{\pi}{4}\right) - 2$

A: -243

~~Amplitude:~~

Reflected over midline? Yes

Vertical Displacement: -2

Midline:  $y = -2$

Phase Shift:  $-\frac{3\pi}{4}$

Period:  $\frac{2\pi}{\frac{1}{3}} = 6\pi$

# Graphs & Inverses of Trig Functions

## 6- Graphing Secant & Cosecant

Write an equation of the secant function with the given information.

- #1)  $A = 3$ , period =  $720^\circ$ ,  
phase shift =  $60^\circ$ ,  $VD = 2$

$$y = 3 \sec\left[\frac{1}{2}(\theta - 60^\circ)\right] + 2$$

$$720^\circ k = 360^\circ$$

$$k = \frac{1}{2}$$

Start with a compound inequality

$$(\text{phase shift})^\circ \leq \theta \leq (\text{phase shift} + \text{period})^\circ.$$

Use your algebra skills to change the equation so it is in the form  $0^\circ \leq \beta \leq p^\circ$ .  
 $p$  = period of parent

The answer will be of this form:  
 $y = \pm \text{Amp} \sin(\beta) + VD$

Write an equation of the cosecant function with the given information.

- #1)  $A = -1$ , period =  $4\pi$ ,  
phase shift =  $-\frac{\pi}{2}$ ,  $VD = 0$

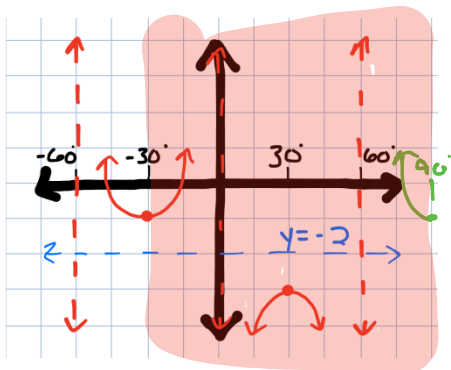
$$y = -\csc\left(\frac{1}{2}\theta + \frac{\pi}{4}\right)$$

$$y = -\csc\left[\frac{1}{2}(\theta + \frac{\pi}{2})\right]$$

$$4\pi k = 2\pi$$

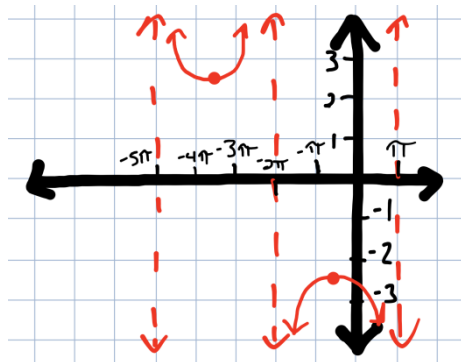
$$k = \frac{1}{2}$$

#2)



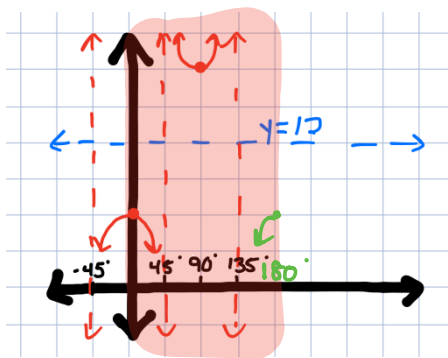
$$y = \sec[3(\theta + 30^\circ)] - 2$$

#2)



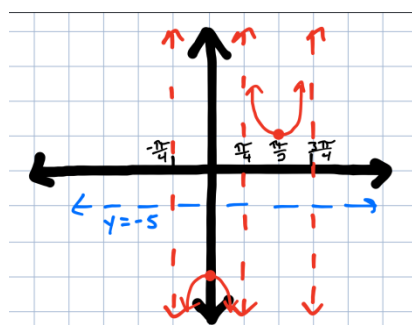
$$y = 2.5 \csc\left[\frac{1}{3}(\theta + 5\pi)\right]$$

#3)



$$y = -6 \sec(2\theta) + 17$$

#3)



$$y = -10 \csc\left[2\left(\theta + \frac{\pi}{4}\right)\right] - 5$$

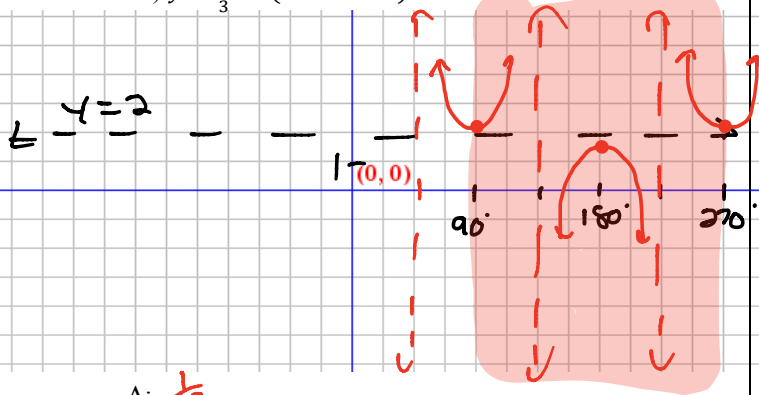
# Graphs & Inverses of Trig Functions

## 6 - Graphing Secant & Cosecant

Graph a minimum of one period for each function.

$$y = \frac{1}{3} \sec[\frac{2}{3}(\theta - 90^\circ)] + 2$$

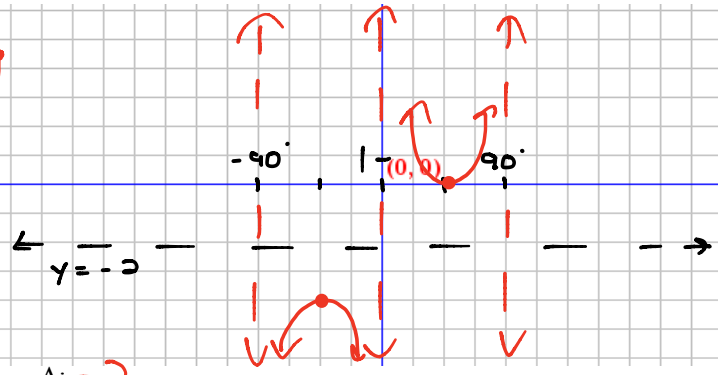
#1)  $y = \frac{1}{3} \sec(2\theta - 180^\circ) + 2$



- A:  $\frac{1}{3}$
- ~~Amplitude:~~
- Reflected over x-axis? **NO**
- Vertical Displacement: **2**
- Midline:  $y = 2$
- Phase Shift:  $90^\circ$
- Period:  $\frac{360^\circ}{2} = 180^\circ$

$$y = -2 \csc[\frac{2}{3}(\theta + 90^\circ)] - 2$$

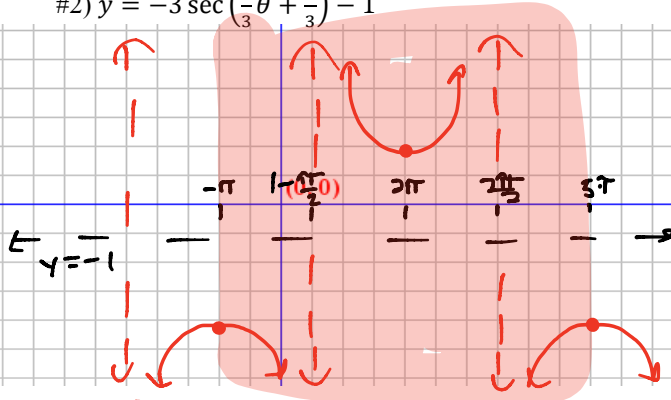
#3)  $y = -2 \csc(2\theta + 180^\circ) - 2$



- A: **-2**
- ~~Amplitude:~~
- Reflected over midline? **Yes**
- Vertical Displacement: **-2**
- Midline:  $y = -2$
- Phase Shift:  $-90^\circ$
- Period:  $\frac{2\pi}{2} = \pi$

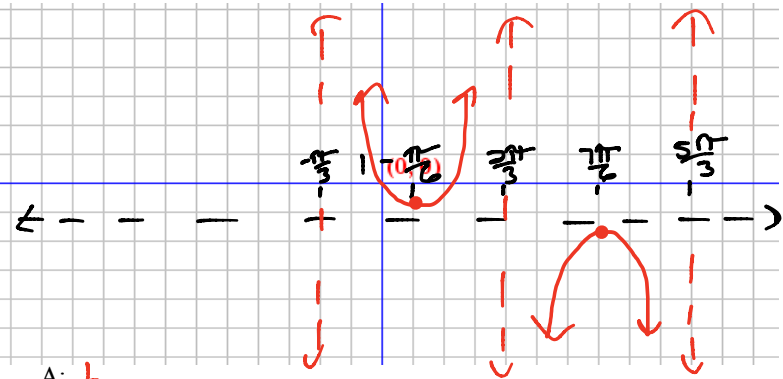
$$y = -3 \sec[\frac{1}{3}(\theta + \pi)] - 1$$

#2)  $y = -3 \sec(\frac{1}{3}\theta + \frac{\pi}{3}) - 1$



- A: **-3**
- ~~Amplitude:~~
- Reflected over x-axis? **Yes**
- Vertical Displacement: **-1**
- Midline:  $y = -1$
- Phase Shift:  $-\pi$
- Period:  $\frac{2\pi}{\frac{1}{3}} = 6\pi$

#4)  $y = \frac{1}{2} \csc(\theta + \frac{\pi}{3}) - 1$



- A:  $\frac{1}{2}$
- ~~Amplitude:~~
- Reflected over midline? **NO**
- Vertical Displacement: **-1**
- Midline:  $y = -1$
- Phase Shift:  $-\frac{\pi}{3}$
- Period:  $2\pi$